

The Seven Crystal Systems

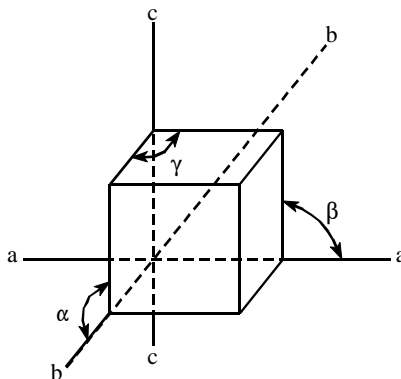
Cubic cell dimensions:

$$a = b = c$$

$$\alpha = \beta = \gamma = 90^\circ$$

(three mutually perpendicular
axes of equal lengths)

This cell is a perfect cube.



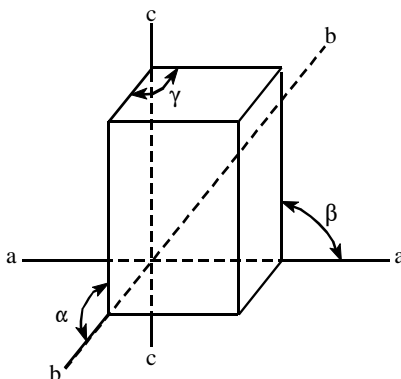
Tetragonal cell dimensions:

$$a = b \neq c$$

$$\alpha = \beta = \gamma = 90^\circ$$

(three mutually perpendicular
axes; two of equal lengths
and one unequal)

This cell is like a saltine-cracker box.



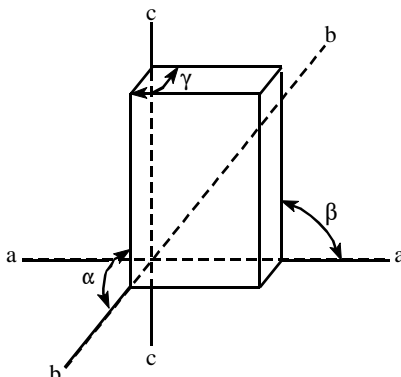
Orthorhombic cell dimensions:

$$a \neq b \neq c$$

$$\alpha = \beta = \gamma = 90^\circ$$

(three mutually perpendicular
axes; two of equal lengths
and one unequal)

This cell is like a shoe box.



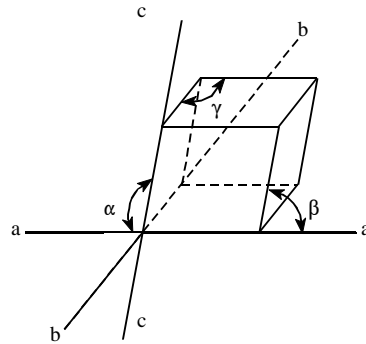
Rhombohedral cell dimensions:

$$a = b = c$$

$$\alpha = \beta = \gamma \neq 90^\circ$$

(two mutually non-perpendicular axes; third axis is perpendicular to one axis but not perpendicular to other; axes of equal lengths)

This cell is like a cube tilted twice.



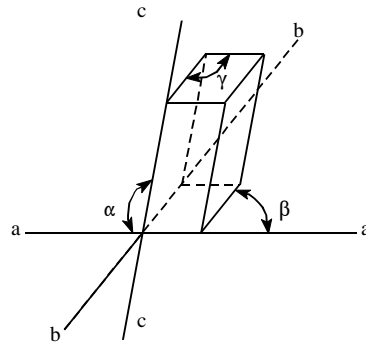
Monoclinic cell dimensions:

$$a \neq b \neq c$$

$$\alpha = \gamma = 90^\circ \quad \beta \neq 90^\circ$$

(two mutually non-perpendicular axes; third axis is perpendicular to one axis but not perpendicular to other; axes of unequal lengths)

This cell is like a shoe box tilted once.



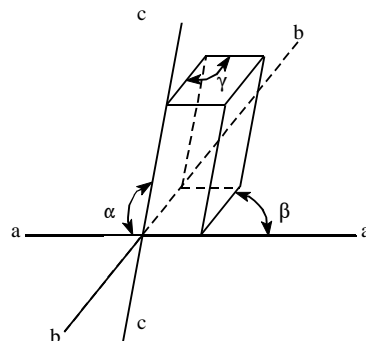
Triclinic cell dimensions:

$$a \neq b \neq c$$

$$\alpha \neq \beta \neq \gamma \neq 90^\circ$$

(three mutually non-perpendicular axes of unequal lengths)

This cell is like a shoe box tilted twice.



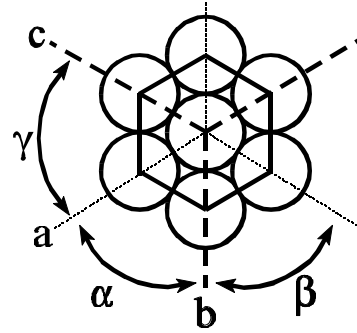
Hexagonal cell dimensions:

$$a = b = c \neq d$$

$$\alpha = \beta = \gamma = 60^\circ; \delta = 90^\circ$$

(three axes of equal length at 60° to each other;
one axis of unequal length at 90° to the other
three axes)

This cell is like a saltine-cracker box compressed
at opposite corners.



Note: There are three unit cells shown.
In each unit cell, there are parts
of eight atoms at the corners of
each unit cell. For the atoms at
the 30° corners only $1/12$ of the
atoms are in the cell while $1/6$
of each atom at the 60° angles
are in the cell. Therefore there
are a total of 2 atoms in each cell.

